

## 1.5 The Exponent Rules

MATHPOWER™ Nine, pp. 20–21

To multiply powers with the same base, add the exponents.

$$y^m \times y^n = y^{m+n}$$

To divide powers with the same base, subtract the exponents.

$$y^m \div y^n = y^{m-n}$$

To raise a power to a power, multiply the exponents.

$$(y^m)^n = y^{m \times n}$$

*Simplify.*

$$\underline{4^6 \times 4^2} \\ 4^8$$

$$\underline{3^5 \times 3^3} \\ 3^8$$

$$\underline{2^2 \times 2^3} \\ 2^5$$

$$\underline{10^3 \times 10} \\ 10^4$$

$$\underline{5^4 \times 5^3} \\ 5^7$$

$$\underline{6 \times 6^4} \\ 6^5$$

$$\underline{x^2 \times x^5} \\ x^7$$

$$\underline{y^3 \times y^3} \\ y^6$$

$$\underline{z^3 \times z^2} \\ z^5$$

*Find the missing exponent.*

$$10. 3^2 \times 3^{\square} = 3^4 \quad \underline{2} \quad 11. 5^{\square} \times 5^4 = 5^7 \quad \underline{3}$$

$$12. 8^3 \times 8^{\square} = 8^5 \quad \underline{2} \quad 13. 7^{\square} \times 7^3 = 7^4 \quad \underline{1}$$

$$14. y^5 \times y^{\square} = y^8 \quad \underline{3} \quad 15. b^{\square} \times b^5 = b^9 \quad \underline{4}$$

$$16. x \times x^9 = x^{\square} \quad \underline{10} \quad 17. s^6 \times s^{\square} = s^7 \quad \underline{1}$$

*Simplify.*

$$\underline{5^4 \div 5^2} \\ 5^2$$

$$\underline{4^6 \div 4^3} \\ 4^3$$

$$\underline{3^3 \div 3^2} \\ 3$$

$$\underline{9^5 \div 9^2} \\ 9^3$$

$$\underline{7^4 \div 7^3} \\ 7$$

$$\underline{2^6 \div 2^4} \\ 2^2$$

$$\underline{x^7 \div x^5} \\ x^2$$

$$\underline{y^8 \div y^6} \\ y^2$$

$$\underline{a^5 \div a^4} \\ a$$

*Find the missing exponent.*

$$27. 2^5 \div 2^{\square} = 2^3 \quad \underline{2} \quad 28. 3^4 \div 3^{\square} = 3^2 \quad \underline{2}$$

$$29. 4^{\square} \div 4^2 = 4^4 \quad \underline{2} \quad 30. 5^{\square} \div 5^3 = 5^{\square} \quad \underline{4}$$

$$31. n^4 \div n^{\square} = n^2 \quad \underline{2} \quad 32. c^{\square} \div c^4 = c^3 \quad \underline{7}$$

$$33. y^{\square} \div y^2 = y^2 \quad \underline{4} \quad 34. z^9 \div z^{\square} = z \quad \underline{8}$$

*Simplify.*

$$\underline{(3^2)^3} \\ 3^6$$

$$\underline{(2^4)^2} \\ 2^8$$

$$\underline{(7^3)^4} \\ 7^{12}$$

$$\underline{(6^2)^4} \\ 6^8$$

$$\underline{(5^3)^2} \\ 5^6$$

$$\underline{(4^5)^3} \\ 4^{15}$$

$$\underline{(x^3)^3} \\ x^9$$

$$\underline{(s^2)^2} \\ s^4$$

$$\underline{(r^5)^2} \\ r^{10}$$

*Find the missing exponent.*

$$44. (3^3)^{\square} = 3^9 \quad \underline{3} \quad 45. (2^5)^{\square} = 2^{10} \quad \underline{2}$$

$$46. (5^{\square})^2 = 5^8 \quad \underline{4} \quad 47. (4^{\square})^3 = 4^{12} \quad \underline{4}$$

$$48. (g^2)^{\square} = g^6 \quad \underline{3} \quad 49. (m^3)^{\square} = m^9 \quad \underline{3}$$

$$50. (s^{\square})^5 = s^{20} \quad \underline{4} \quad 51. (t^{\square})^2 = t^6 \quad \underline{3}$$

*Find the value of each expression.*

Replace the blanks with the corresponding letter or symbol to decode the message.

$$52. 2^3 \times 2^2 \quad C \quad 53. 2^9 \div 2^2 \quad R$$

$$54. 2^4 \div 2^3 \quad A \quad 55. (2^3)^2 \quad O$$

$$56. 2^{13} \div 2^3 \quad C \quad 57. (2^6)^2 \quad !$$

$$58. 2 \times 2 \quad L \quad 59. (2^4)^2 \quad R$$

$$60. 2^2 \times 2^2 \quad * \quad 61. 2^2 \times 2 \quad L$$

$$62. (2^3)^3 \quad E \quad 63. 2^{12} \div 2 \quad T$$

$$\frac{A}{2^1} \frac{L}{2^2} \frac{L}{2^3} \frac{L}{2^4} \frac{C}{2^5} \frac{Q}{2^6} \frac{Q}{2^7} \frac{Q}{2^8} \frac{E}{2^9} \frac{C}{2^{10}} \frac{T}{2^{11}} \frac{!}{2^{12}}$$

## 1.8 Working with Exponents

MATHPOWER™ Nine, pp. 26–29

To multiply powers with the same integral base, add the exponents.

$$x^m \times x^n = x^{m+n}$$

To divide powers with the same integral base, subtract the exponents.

$$x^m \div x^n = x^{m-n}$$

To raise a power with an integral base to a power, multiply the exponents.

$$(x^m)^n = x^{m \times n}$$

Complete the table.

Exponential Form	Base	Exponent	Standard Form
1. $(-2)^3$	-2	3	-8
2. $3^1$	3	1	3
3. $5^4$	5	4	625
4. $(-3)^3$	-3	3	-27
5. $(-2)^5$	-2	5	-32
6. $7^2$	7	2	49

Complete the table.

Exponential Form	Repeated Multiplication	Standard Form
7. $(-3)^2 \times (-3)^2$	$(-3)(-3)(-3)(-3)$	81
8. $(-4)^3$	$(-4) \times (-4) \times (-4)$	-64
9. $(-5)^3$	$(-5)(-5)(-5)$	-125
10. $(-4)^3 \div (-4)$	$\frac{(-4) \times (-4) \times (-4)}{(-4)}$	16
11. $(+5)^4 \div (+5)^2$	$\frac{(+5)(+5)(+5)(+5)}{(+5)(+5)}$	25
12. $(+5)^3$	$(+5) \times (+5) \times (+5)$	125
13. $(-3)^5 \div (-3)^2$	$\frac{(-3)(-3)(-3)(-3)(-3)}{(-3)(-3)}$	-27
14. $(-2)^5$	$(-2) \times (-2) \times (-2) \times (-2) \times (-2)$	-32

Write in standard form.

15.  $3^2 \times 3^3$  243    16.  $(-2)^3 \times (-2)^2$  -32
17.  $(5)^4(5)^3$  78125    18.  $(3.2)^2(3.2)^2$  104.8576
19.  $((y)^2)^3$   $y^6$     20.  $(3)^4 \div (3)^2$  9
21.  $((-4.5)^2)^5$  3405062.322    22.  $(-5)^3 \div (-5)$  25
23.  $\frac{3^5}{3^3}$  9    24.  $\frac{(-7)^3}{(-7)^2}$  -7

Is each statement true or false?

25.  $3^3 = 81$  F    26.  $6(-2)^3 = 48$  F
27.  $(-4)^2 \times (-4)^2 = -64$  F
28.  $y^2 \times y^4 = y^6$  T
29.  $(-a)^4 \div (-a)^2 = a^2$  T
30.  $(-5)^3 \div (-5)^2 = 5$  F

Evaluate for  $s = -3$  and  $t = 2$ .

31.  $t^3$  8    32.  $\frac{6}{s^2}$   $\frac{6}{9}$
33.  $s^3 + t^2$  -23    34.  $2s^3 \div 3t$  -9
35.  $-3st$  18    36.  $-2s^2 - 4t$  26

37. The formula for the volume,  $V$ , of a sphere is  $V = 4.19r^3$ , where  $r$  is the radius. Complete the table.

Radius (m)	Volume ( $m^3$ )
4	268.16
7	1437.17
2	33.52
2.3	50.98
10	4130

38. If the base of a power is negative and the exponent is five, the standard form of the number is negative. Explain.

If the power is odd the negative is multiplied an odd number of times and remains negative.

39. The standard forms of the following terms are not the same. Explain why this is true.

$(-2)^4$  16     $-2^4$  -16  
 With the brackets the answer is five, without it it is eight.