

Simple and Compound interest

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Simple interest

$$I = Prt$$

I interest earned

P amount of money started with (Principle)

r interest rate as a decimal

t time in years.

1) You invest \$400 at 3% interest for 2 years. How much interest do you earn?

$$P = 400$$

$$r = 0.03$$

$$t = 2$$

$$\begin{aligned} I &= Prt \\ &= (400)(0.03)(2) \\ &= \$24 \end{aligned}$$

2) You invest \$1000 at 2.5% interest for 6 months. How much is your investment worth at the end?

$$P = 1000$$

$$r = 0.025$$

$$t = 6 \text{ months}$$

$$= 0.5 \text{ years}$$

$$\begin{aligned} I &= Prt \\ &= (1000)(0.025)(0.5) \\ &= \$12.50 \end{aligned}$$

$$\begin{aligned} A &= P + I \\ &= \$1000 + \$12.50 \\ &= \$1012.50 \end{aligned}$$

3) You invest \$500 at 4% interest. You earn \$20 interest. How long was the amortization period?

$$P = 500$$

$$r = 0.04$$

$$I = 20$$

$$\frac{I = Prt}{Pr} \Rightarrow$$

$$\begin{aligned} t &= \frac{I}{Pr} \\ &= \frac{20}{(500 \times 0.04)} \\ &= 1 \end{aligned}$$

4) You earn \$35 after investing for 2.5 years at 0.25% interest.
How much did you invest?

$$t = 2.5$$

$$r = 0.0025$$

$$I = 35$$

$$\frac{I}{rt} = \frac{Prt}{rt} \Rightarrow P = \frac{I}{rt}$$

$$= \frac{35}{[(0.0025)(2.5)]}$$

$$= \$5600$$

5) You earn \$125 on a \$650 investment, invested for 7 yrs.
What was the interest rate?

$$I = 125$$

$$P = 650$$

$$t = 7$$

$$\frac{I}{Pt} = \frac{Prt}{Pt} \Rightarrow r = \frac{I}{Pt} \times 100$$

$$= \frac{125}{(650 \times 7)} \times 100$$

$$= 2.7\%$$

Compound interest

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

A actual amount principle and interest together.

P principle

r interest rate as a decimal

t term in years

n Compounding period

-how many times compounded each year.

yearly $n=1$ semi-annually $n=2$ quarterly $n=4$
monthly $n=12$ weekly $n=52$

D) You invest \$1000 at 1.5% interest, **compounded** quarterly for 2 years. How much is your investment worth after 2 years?

$$P = 1000$$

$$n = 4$$

$$t = 2$$

$$r = 0.015$$

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

$$= 1000 \times \left(1 + \frac{0.015}{4}\right)^{(4 \times 2)}$$

$$= 1030.40$$